

G5. Derivate - Esercizi:

Calcola la derivata delle seguenti funzioni

- | | | |
|-----|-------------------------------------|--|
| 1) | $y = \sin(\pi/2)$ | $[y' = 0]$ |
| 2) | $y = 5^x$ | $[y' = 5^x \cdot \ln 5]$ |
| 3) | $y = 3x$ | $[y' = 3]$ |
| 4) | $y = -\frac{1}{2} \sin x$ | $[y' = -\frac{1}{2} \cos x]$ |
| 5) | $y = e$ | $[y' = 0]$ |
| 6) | $y = \frac{1}{3} \ln x$ | $[y' = \frac{1}{3x}]$ |
| 7) | $y = -\frac{1}{2}$ | $[y' = 0]$ |
| 8) | $y = e^x - 2 \cdot \ln x$ | $[y' = e^x - \frac{2}{x}]$ |
| 9) | $y = 2\pi$ | $[y' = 0]$ |
| 10) | $y = \ln x$ | $[y' = \frac{1}{x}]$ |
| 11) | $y = -2e^x$ | $[y' = -2e^x]$ |
| 12) | $y = \log_3 x$ | $[y' = \frac{1}{x} \log_3 e]$ |
| 13) | $y = -2 \log_a x$ | $[y' = -\frac{2}{x} \log_a e]$ |
| 14) | $y = 3x - 5 \cdot \cos x$ | $[y' = 3 + 5 \sin x]$ |
| 15) | $y = 3 \cos x$ | $[y' = -3 \sin x]$ |
| 16) | $y = 5 \cdot 3^x$ | $[y' = 5 \cdot 3^x \cdot \ln 3]$ |
| 17) | $y = -x - 2 \ln x$ | $[y' = -1 - \frac{2}{x}]$ |
| 18) | $y = 4x + 2 \log x - 2$ | $[y' = 4 + \frac{2}{x} \log e]$ |
| 19) | $y = \sin x + 2 \cos x$ | $[y' = \cos x - 2 \sin x]$ |
| 20) | $y = 5^x + 3^x - 2$ | $[y' = 5^x \cdot \ln 5 + 3^x \cdot \ln 3]$ |
| 21) | $y = 3x + \ln x$ | $[y' = 3 + \frac{1}{x}]$ |
| 22) | $y = x^2 \cdot e^x$ | $[y' = e^x \cdot (2x + x^2)]$ |
| 23) | $y = 4^x + \log_4 x$ | $[y' = 4^x \cdot \ln 4 + \frac{1}{x} \log_4 e]$ |
| 24) | $y = 2 \sin x \cos x$ | $[y' = 2(\cos^2 x - \sin^2 x)]$ |
| 25) | $y = 2^x \cdot \sin x$ | $[y' = 2^x(\ln 2 \cdot \sin x + \cos x)]$ |
| 26) | $y = 5x^2 - \frac{3}{x^3}$ | $[y' = 10x + \frac{9}{x^4}]$ |
| 27) | $y = x^{\frac{1}{3}}$ | $[y' = \frac{1}{3} x^{-\frac{2}{3}}]$ |
| 28) | $y = (3x + 2 \ln x) \cdot \sin x$ | $[y' = \left(3 + \frac{2}{x}\right) \cdot \sin x + (3x + 2 \ln x) \cdot \cos x]$ |
| 29) | $y = x^7$ | $[y' = 7x^6]$ |
| 30) | $y = \frac{1}{x^3} - \frac{3}{x^4}$ | $[y' = -\frac{3}{x^4} + \frac{12}{x^5}]$ |
| 31) | $y = \frac{1}{\sqrt[3]{x^2}}$ | $[y' = -\frac{2}{3x \cdot \sqrt[3]{x^2}}]$ |
| 32) | $y = -\frac{1}{5} x^5$ | $[y' = -x^4]$ |
| 33) | $y = 5x \cdot e^x \cdot \cos x$ | $[y' = 5e^x \cdot (\cos x + x \cos x - x \sin x)]$ |
| 34) | $y = 5e^x \cdot \cos x$ | $[y' = 5e^x \cdot (\cos x - \sin x)]$ |
| 35) | $y = 3x^5 - 2x^2 + 4$ | $[y' = 15x^4 - 4x]$ |
| 36) | $y = \sin x - x \cdot \ln x$ | $[y' = \cos x - \ln x - 1]$ |
| 37) | $y = (e^x + 2x) \cdot \ln x$ | $[y' = e^x \ln x + 2 \ln x + \frac{e^x}{x} + 2]$ |

- 38) $y = e^x \cdot \ln x$ $[y' = e^x \cdot (\ln x + \frac{1}{x})]$
- 39) $y = 2x^2 \cdot \operatorname{tg} x$ $[y' = 2x \cdot (2\operatorname{tg} x + \frac{x}{\cos^2 x})]$
- 40) $y = 5x^4 - 3x^3 + 2x^2 + x$ $[y' = 20x^3 - 9x^2 + 4x + 1]$
- 41) $y = -\frac{2}{x^2}$ $[y' = \frac{4}{x^3}]$
- 42) $y = \sqrt[3]{x^4} - 2x^2 + 5x$ $[y' = \frac{4 \cdot \sqrt[3]{x}}{3} - 4x + 5]$
- 43) $y = -3x^3$ $[y' = -9x^2]$
- 44) $y = \sqrt[4]{x}$ $[y' = \frac{1}{4 \cdot \sqrt[4]{x^3}}]$
- 45) $y = \frac{1}{2}x^6 - \frac{1}{4}x^4 + x^2$ $[y' = 3x^5 - x^3 + 2x]$
- 46) $y = -x^5$ $[y' = -5x^4]$
- 47) $y = \frac{\sqrt{x}}{x}$ $[y' = -\frac{1}{2x \cdot \sqrt{x}}]$
- 48) $y = 2x^3 + 3x^2$ $[y' = 6x^2 + 6x]$
- 49) $y = \sqrt[5]{x^2} - 5x^2$ $[y' = \frac{2}{5 \cdot \sqrt[5]{x^3}} - 10x]$
- 50) $y = 3\sqrt{x} - \frac{3}{x}$ $[y' = \frac{3}{2 \cdot \sqrt{x}} + \frac{3}{x^2}]$
- 51) $y = \frac{x^2 - 2x + 3}{x^2 - 1}$ $[y' = \frac{2(x^2 - 4x + 1)}{(x^2 - 1)^2}]$
- 52) $y = \frac{3}{x^3 - 1}$ $[y' = \frac{-9x^2}{(x^3 - 1)^2}]$
- 53) $y = \sqrt[3]{3x^3 - 2x}$ $[y' = \frac{9x^2 - 2}{3 \cdot \sqrt[3]{(3x^3 - 2x)^2}}]$
- 54) $y = \cos(x^4)$ $[y' = -4x^3 \cdot \operatorname{sen}(x^4)]$
- 55) $y = \cos^4 x$ $[y' = -4 \operatorname{sen} x \cos^3 x]$
- 56) $y = \frac{5}{(1 - 2x)^2}$ $[y' = \frac{20}{(1 - 2x)^3}]$
- 57) $y = (x^2 - x)^2$ $[y' = 2x(x - 1)(2x - 1)]$
- 58) $y = \frac{\sqrt{x^2 + 1}}{e^x}$ $[y' = \frac{-x^2 + x - 1}{e^x \cdot \sqrt{x^2 + 1}}]$
- 59) $y = \frac{2 - \ln x}{x}$ $[y' = \frac{-\ln x - 3}{x^2}]$
- 60) $y = \operatorname{cotg} x$ $[y' = -1 - \operatorname{cotg}^2 x = -\frac{1}{\operatorname{sen}^2 x}]$
- 61) $y = \frac{\cos x - 1}{x^2}$ $[y' = \frac{-x \operatorname{sen} x - 2 \cos x + 2}{x^3}]$
- 62) $y = (x + 2)^4$ $[y' = 4 \cdot (x + 2)^3]$
- 63) $y = e^x + 5x \cdot \ln x$ $[y' = e^x + 5 \ln x + 5]$
- 64) $y = \frac{1}{x^2 - 1}$ $[y' = \frac{-2x}{(x^2 - 1)^2}]$
- 65) $y = (\ln x + 1)^6$ $[y' = 6(\ln x + 1)^5 \cdot \frac{1}{x}]$
- 66) $y = -\frac{1}{x^3} + 2\pi$ $[y' = \frac{3}{x^4}]$
- 67) $y = x + \ln^2 x$ $[y' = 1 + \frac{2}{x} \ln x]$

68)	$y = x + \ln(x^2)$	$[y' = 1 + \frac{2}{x}]$
69)	$y = x \cdot \ln^2 x$	$[y' = \ln^2 x + 2 \ln x]$
70)	$y = x \cdot \ln(x^2)$	$[y' = \ln(x^2) + 2]$
71)	$y = \frac{2x - 3}{x^2 - 1}$	$[y' = \frac{-2x^2 + 6x - 2}{(x^2 - 1)^2}]$
72)	$y = (2x^5 - 3)^2$	$[y' = 20x^4(2x^5 - 3)]$
73)	$y = \sqrt{x} \cdot \sin^2 x$	$[y' = \frac{\sin^2 x + 4x \sin x \cos x}{2 \cdot \sqrt{x}}]$
74)	$y = (3x^2 - 1)^3$	$[y' = 18x(3x^2 - 1)^2]$
75)	$y = \sqrt[5]{x^2 - 1}$	$[y' = \frac{2x}{5 \cdot \sqrt[5]{(x^2 - 1)^4}}]$
76)	$y = \frac{x + 1}{2x - 1}$	$[y' = \frac{-3}{(2x - 1)^2}]$
77)	$y = \sqrt[4]{x^3 + x^2 + 2x}$	$[y' = \frac{3x^2 + 2x + 2}{4 \cdot \sqrt[4]{(x^3 + x^2 + 2x)^3}}]$
78)	$y = \sqrt{x - 3}$	$[y' = \frac{1}{2 \cdot \sqrt{x - 3}}]$
79)	$y = (2 + \cos x)^3$	$[y' = -3 \sin x (2 + \cos x)^2]$
80)	$y = \frac{x^2}{x^2 - 1}$	$[y' = \frac{-2x}{(x^2 - 1)^2}]$
81)	$y = e^{\frac{x}{x^2 - 1}}$	$[y' = e^{\frac{x}{x^2 - 1}} \cdot \frac{-x^2 - 1}{(x^2 - 1)^2}]$
82)	$y = \frac{2x + \sin x}{\sin x}$	$[y' = \frac{2(\sin x - x \cos x)}{\sin^2 x}]$
83)	$y = \frac{x^3}{1 - x^4}$	$[y' = \frac{x^6 + 3x^2}{(1 - x^4)^2}]$
84)	$y = \frac{x^2 + 1}{(x + 1)^2}$	$[y' = \frac{2x - 2}{(x + 1)^3}]$
85)	$y = \frac{x^3}{(x^2 - 1)^2}$	$[y' = \frac{-3x^2 - x^4}{(x^2 - 1)^3}]$
86)	$y = \frac{3x^4 - 2}{e^x}$	$[y' = \frac{-3x^4 + 12x^3 + 2}{e^x}]$
87)	$y = \frac{x^4}{2x + 3}$	$[y' = \frac{6x^4 + 12x^3}{(2x + 3)^2}]$
88)	$y = e^{\sqrt{x}}$	$[y' = \frac{e^{\sqrt{x}}}{2 \cdot \sqrt{x}}]$
89)	$y = \frac{\sqrt[4]{x^3}}{\sqrt{x}}$	$[y' = \frac{1}{4 \cdot \sqrt[4]{x^3}}]$
90)	$y = \frac{1}{\ln^3 x}$	$[y' = \frac{-3}{x \cdot \ln^4 x}]$
91)	$y = \frac{3x - 2}{x^3}$	$[y' = \frac{-6x + 6}{x^4}]$
92)	$y = \frac{\sin x}{x}$	$[y' = \frac{x \cos x - \sin x}{x^2}]$
93)	$y = 2 \cdot 3^x + 3$	$[y' = 2 \cdot 3^x \cdot \ln 3]$
94)	$y = \ln(3x - 1)$	$[y' = \frac{3}{3x - 1}]$
95)	$y = e^{x-2}$	$[y' = e^{x-2}]$
96)	$y = \sqrt{\operatorname{tg} x}$	$[y' = \frac{1 + \operatorname{tg}^2 x}{2 \cdot \sqrt{\operatorname{tg} x}}]$

97)	$y = \frac{\ln x}{\operatorname{tg} x}$	$[y' = \frac{\operatorname{tg} x - x \cdot \ln x - x \cdot \ln x \cdot \operatorname{tg}^2 x}{x \cdot \operatorname{tg}^2 x}]$
98)	$y = \operatorname{tg}^2 x$	$[y' = 2 \operatorname{tg} x (1 + \operatorname{tg}^2 x)]$
99)	$y = \frac{x \cdot \operatorname{sen} x}{e^x}$	$[y' = \frac{\operatorname{sen} x + x \operatorname{cos} x - x \operatorname{sen} x}{e^x}]$
100)	$y = \frac{\ln x}{x}$	$[y' = \frac{1 - \ln x}{x^2}]$

Risolvere i limiti seguenti utilizzando la regola di De L'Hôpital.

101)	$\lim_{x \rightarrow \infty} \frac{x^2 - 2x}{3x}$	$[\infty]$
102)	$\lim_{x \rightarrow \infty} \frac{2 - x^2}{x^2}$	$[-1]$
103)	$\lim_{x \rightarrow \infty} \frac{5 - 3x}{2x}$	$[-\frac{3}{2}]$
104)	$\lim_{x \rightarrow \infty} \frac{2x - 1}{x^2 - 1}$	$[0]$
105)	$\lim_{x \rightarrow \infty} \frac{x^2 + 3x + 4}{x^4 - x^2}$	$[0]$
106)	$\lim_{x \rightarrow \infty} \frac{x^2 - 8x^3}{x^2}$	$[\infty]$
107)	$\lim_{x \rightarrow 1} \frac{x - 1}{x^3 - 1}$	$[\frac{1}{3}]$
108)	$\lim_{x \rightarrow 2} \frac{x - 2}{\sqrt{x} - \sqrt{2}}$	$[2 \cdot \sqrt{2}]$
109)	$\lim_{x \rightarrow -1} \frac{1 + x}{x^2 + 1 + 2x}$	$[\infty]$
110)	$\lim_{x \rightarrow 3} \frac{x^2 - 6x + 9}{x^2 - 5x + 6}$	$[0]$
111)	$\lim_{x \rightarrow -2} \frac{x^2 + 6x + 8}{x^2 - 4}$	$[-\frac{1}{2}]$
112)	$\lim_{x \rightarrow \infty} \frac{e^x + x^2}{x^2 - x}$	$[\infty]$
113)	$\lim_{x \rightarrow \infty} \frac{3e^x - x}{2x - e^x}$	$[-3]$
114)	$\lim_{x \rightarrow \infty} \frac{2^x}{\ln x}$	$[\infty]$
115)	$\lim_{x \rightarrow 0} \frac{e^x - 1}{x}$	$[1]$
116)	$\lim_{x \rightarrow 0} \frac{\operatorname{sen} x}{x}$	$[1]$
117)	$\lim_{x \rightarrow 0} \frac{x^2}{1 - \operatorname{cos} x}$	$[2]$
118)	$\lim_{x \rightarrow 0} \frac{\operatorname{tg} x}{x^2}$	$[\infty]$
119)	$\lim_{x \rightarrow 1} \frac{\ln x}{x - 1}$	$[1]$
120)	$\lim_{x \rightarrow 2} \frac{\ln(x - 1)}{\operatorname{sen}(x - 2)}$	$[1]$
121)	$\lim_{x \rightarrow -2} \frac{3e^{x+2} - 3}{x^2 - 4}$	$[-\frac{3}{4}]$

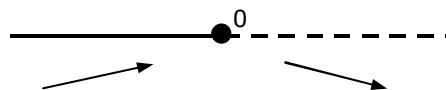
- 122) $\lim_{x \rightarrow -\infty} \frac{1-x^2}{x}$ [$+\infty$]
 123) $\lim_{x \rightarrow 0} \frac{e^x - 1}{\cos^2 x - 1}$ [∞]
 124) $\lim_{x \rightarrow 0} \frac{1 - \cos^2 x}{x^2}$ [1]
 125) $\lim_{x \rightarrow 1} \frac{\cos x - \cos 1}{x - 1}$ [-sen1]

Trova l'equazione della retta tangente alla funzione data passante per il punto di ascissa indicata.

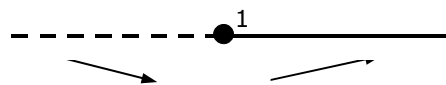
- 126) $y = x^2 - 2x + 1$ $x_0 = 2$ [$y = 2x - 3$]
 127) $y = x^3 + 3x^2$ $x_0 = -1$ [$y = -3x - 1$]
 128) $y = x^3 - 2x + 1$ $x_0 = 0$ [$y = -2x + 1$]
 129) $y = \frac{1}{3}x^3 - \frac{1}{2}x^2 + x$ $x_0 = 1$ [$y = x - \frac{1}{6}$]
 130) $y = \frac{x^2 - 3x}{x - 1}$ $x_0 = 2$ [$y = 3x - 8$]
 131) $y = \frac{x^2 - x + 1}{x^2 - 1}$ $x_0 = 0$ [$y = x - 1$]
 132) $y = \sqrt{2x^2 - 2}$ $x_0 = 1$ [$x = 1$]
 133) $y = \frac{4 - x^2}{x}$ $x_0 = -1$ [$y = -5x - 8$]
 134) $y = -\frac{2}{x}$ $x_0 = \frac{1}{2}$ [$y = 8x - 8$]
 135) $y = 4x^2 - 6x + 9$ $x_0 = 1$ [$y = 2x + 5$]
 136) $y = e^{3x} - 1$ $x_0 = 0$ [$y = 3x$]
 137) $y = x^2 \cdot \ln x$ $x_0 = 1$ [$y = x - 1$]
 138) $y = \frac{1}{2}\sqrt{x^2 - 1}$ $x_0 = \sqrt{2}$ [$y = \frac{\sqrt{2}}{2}x - \frac{1}{2}$]
 139) $y = 2x + e^{x-1}$ $x_0 = 1$ [$y = 3x$]
 140) $y = -x^2 + 4x$ $x_0 = 3$ [$y = -2x + 9$]

Studia la derivata prima delle seguenti funzioni.

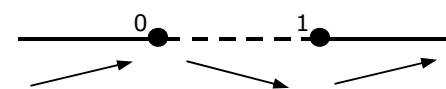
- 141) $y = 2 - x^2$ massimo (0;2)



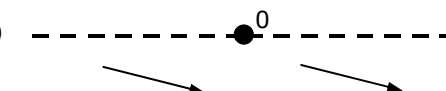
- 142) $y = 2x^2 - 4x$ minimo (1;-2)



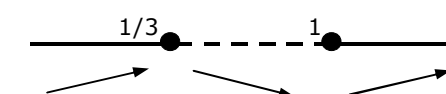
- 143) $y = 2x^3 - 3x^2$ massimo (0;0)
minimo (1;-1)



- 144) $y = -x^3$ flesso disc. a tg orizz.le (0;0)

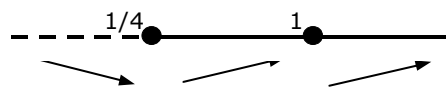


- 145) $y = x \cdot (x-1)^2$ massimo $(\frac{1}{3}; \frac{4}{27})$
minimo (1;0)



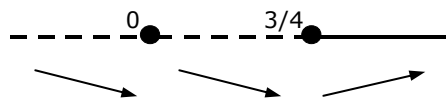
146) $y = x \cdot (x-1)^3$

minimo $\left(\frac{1}{4}; -\frac{27}{256}\right)$
 flesso asc. a tg orizz.le (1;0)



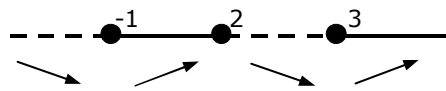
147) $y = x^4 - x^3$

minimo $\left(\frac{3}{4}; -\frac{27}{256}\right)$
 flesso disc. a tg orizz.le (0;0)



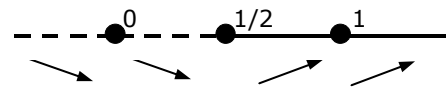
148) $y = \frac{x^4}{4} - 4\frac{x^3}{3} + \frac{x^2}{2} + 6x$

minimo $\left(-1; -\frac{47}{12}\right)$
 massimo $\left(2; \frac{22}{3}\right)$
 minimo $\left(3; \frac{27}{4}\right)$



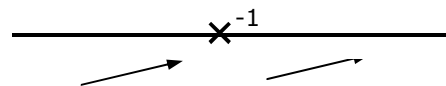
149) $y = x^3 \cdot (x-1)^3$

flesso disc. a tg orizz.le (0;0)
 minimo $\left(\frac{1}{2}; -\frac{1}{64}\right)$
 flesso asc. a tg orizz. (1;0)



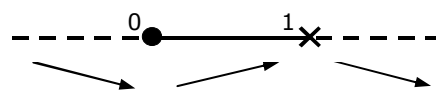
150) $y = \frac{x-1}{x+1}$

nè max, nè min, nè flessi



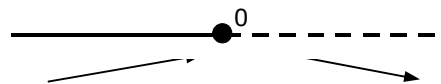
151) $y = \frac{x^2}{(x-1)^2}$

minimo (0;0)



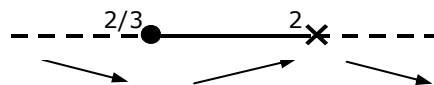
152) $y = \frac{2}{x^2 + 1}$

massimo (0;2)



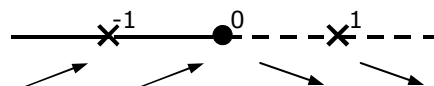
153) $y = \frac{x^2 - x}{x^2 - 4x + 4}$

minimo $\left(\frac{2}{3}; -\frac{1}{8}\right)$



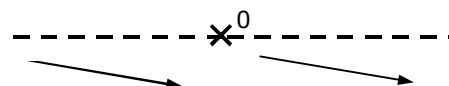
154) $y = \frac{2}{x^2 - 1}$

massimo (0;-2)



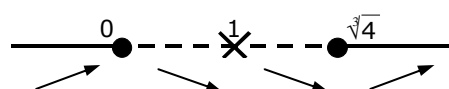
155) $y = \frac{-3}{x^2}$

nè max, nè min, nè flessi



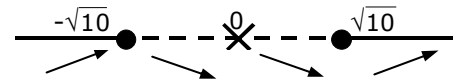
156) $y = \frac{x^4}{x^3 - 1}$

minimo $\left(\sqrt[3]{4}; \frac{4 \cdot \sqrt[3]{4}}{3}\right)$
 massimo (0;0)



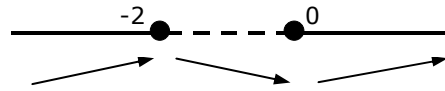
157) $y = \frac{x^2 - 7x + 10}{x}$

massimo $(-\sqrt{10}; -2\sqrt{10} - 7)$
 minimo $(\sqrt{10}; 2\sqrt{10} - 7)$



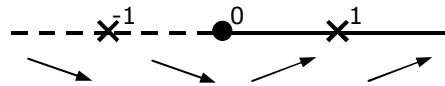
158) $y = \frac{x^2}{1 + x + x^2}$

minimo $(0; 0)$
 massimo $(-2; \frac{4}{3})$



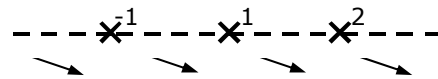
159) $y = \frac{x^2 - 4}{x^2 - 1}$

minimo $(0; 4)$



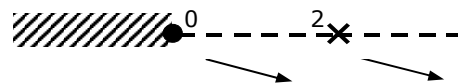
160) $y = \frac{x^2 - 1}{x^3 - 2x^2 - x + 2}$

nè max, nè min, nè flessi



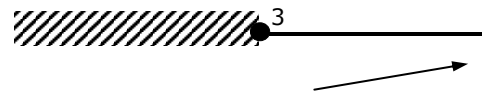
161) $y = \frac{\sqrt{x} - \sqrt{2}}{x - 2}$

massimo $(0; \frac{\sqrt{2}}{2})$



162) $y = \sqrt{x - 3}$

minimo $(3; 0)$



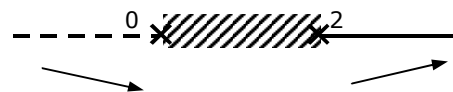
163) $y = \sqrt{x^2 - 1}$

minimo $(-1; 0)$
 minimo $(1; 0)$



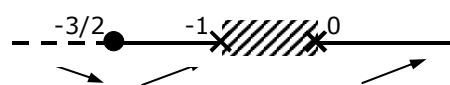
164) $y = \frac{\sqrt{x^2 - 2x}}{x}$

minimo $(2; 0)$



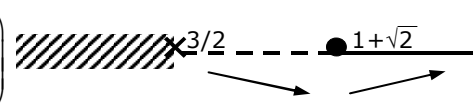
165) $y = \sqrt{\frac{x^3}{x+1}}$

minimo $(-\frac{3}{2}; \frac{3 \cdot \sqrt{3}}{2})$



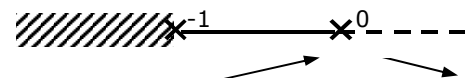
166) $y = \frac{x^2 + 3}{\sqrt{2x - 3}}$

minimo $(1 + \sqrt{2}; \frac{6 + 2\sqrt{2}}{\sqrt{2\sqrt{2} - 1}})$



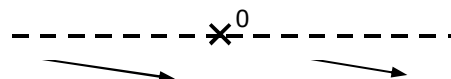
167) $y = \ln\left(\frac{x+1}{x^2}\right)$

nè max, nè min, nè flessi



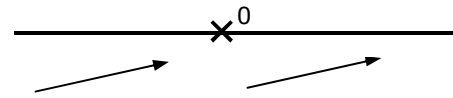
168) $y = \frac{e^x}{e^x - 1}$

nè max, nè min, nè flessi



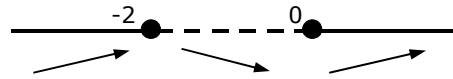
169) $y = \frac{e}{1 + e^{1/x}}$

nè max, nè min, nè flessi



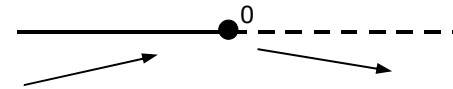
170) $y = x^2 \cdot e^x$

massimo $(-2; \frac{4}{e^2})$
min $(0; 0)$



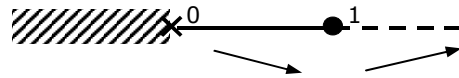
171) $y = e^{-x^2}$

massimo $(0; 1)$



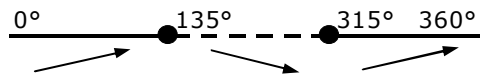
172) $y = \ln x - x$

massimo $(1; -1)$



173) $y = \sin x - \cos x$

massimo $(\frac{3}{4}\pi; \sqrt{2})$
minimo $(\frac{7}{4}\pi; -\sqrt{2})$



Studia la derivata seconda delle seguenti funzioni.

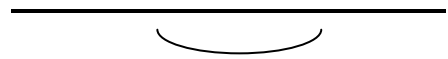
174) $y = 2 - x^2$

non ci sono flessi



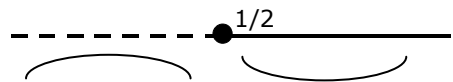
175) $y = 2x^2 - 4x$

non ci sono flessi



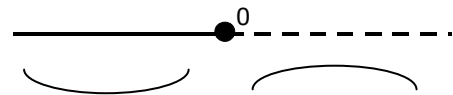
176) $y = 2x^3 - 3x^2$

flesso $(\frac{1}{2}; -\frac{1}{2})$



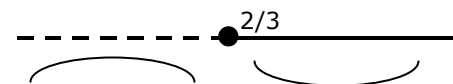
177) $y = -x^3$

flesso $(0; 0)$



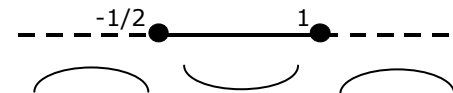
178) $y = x \cdot (x-1)^2$

flesso $(\frac{2}{3}; \frac{2}{27})$



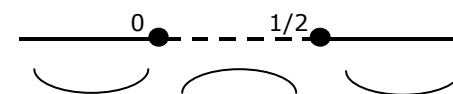
179) $y = x \cdot (x-1)^3$

flessi $(\frac{1}{2}; -\frac{1}{16})$ $(1; 0)$



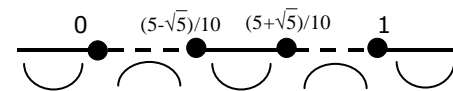
180) $y = x^4 - x^3$

flessi $(0; 0)$ $(\frac{1}{2}; -\frac{1}{16})$



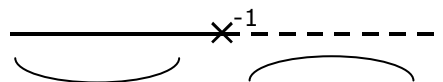
181) $y = x^3 \cdot (x-1)^3$

flessi $(0; 0)$ $(1; 0)$
 $(\frac{5-\sqrt{5}}{10}; \dots)$ $(\frac{5+\sqrt{5}}{10}; \dots)$



182) $y = \frac{x-1}{x+1}$

non ci sono flessi



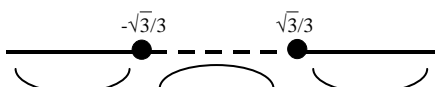
183) $y = \frac{x^2}{(x-1)^2}$

flesso $(-\frac{1}{2}; \frac{1}{9})$



184) $y = \frac{2}{x^2+1}$

flessi $(\frac{-\sqrt{3}}{3}; \frac{3}{2})$ $(\frac{\sqrt{3}}{3}; \frac{3}{2})$



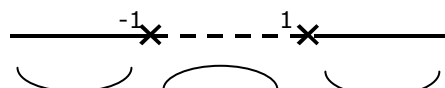
185) $y = \frac{x^2-x}{x^2-4x+4}$

flesso (0;0)



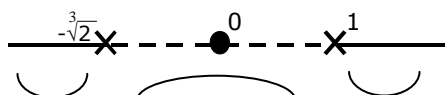
186) $y = \frac{2}{x^2-1}$

non ci sono flessi



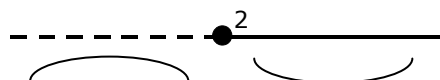
187) $y = \frac{x^4}{x^3-1}$

flesso $(-\sqrt[3]{2}; -\frac{2}{3}\sqrt[3]{2})$



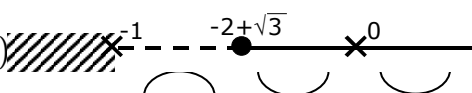
188) $y = x \cdot e^{-x}$

flesso $(2; \frac{2}{e^2})$



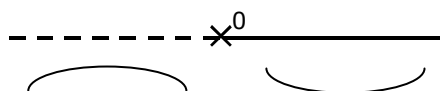
189) $y = \ln\left(\frac{x+1}{x^2}\right)$

flesso $(-2 + \sqrt{3}; \ln(5 + 11\sqrt{3}))$



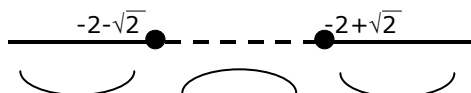
190) $y = \frac{e^x}{e^x-1}$

non ci sono flessi



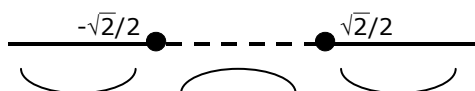
191) $y = x^2 \cdot e^x$

flessi $(-2 - \sqrt{2}; (6 + 4\sqrt{2}) \cdot e^{-2-\sqrt{2}})$
 $(-2 + \sqrt{2}; (6 - 4\sqrt{2}) \cdot e^{-2+\sqrt{2}})$



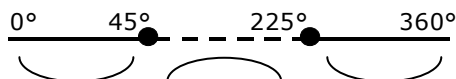
192) $y = e^{-x^2}$

flessi $(\frac{-\sqrt{2}}{2}; \frac{1}{\sqrt{e}})$
 $(\frac{\sqrt{2}}{2}; \frac{1}{\sqrt{e}})$



$y = \sin x - \cos x$

flessi $(\frac{\pi}{4}; 0)$ $(\frac{5\pi}{4}; 0)$



Trova i punti di flesso delle funzioni date e le tangenti in essi.

193) $y = x^3 - x^2$

[fl $(\frac{1}{3}; -\frac{2}{27})$; $y = -\frac{1}{3}x + \frac{1}{27}$]

194) $y = \text{sen}x$

[fl $(0;0)$ $y=x$; fl $(\pi;0)$ $y=-x+\pi$]

195) $y = x \cdot e^{-x}$

[fl $(2; \frac{2}{e^2})$; $y = -\frac{x}{e^2} + \frac{4}{e^2}$]

196) $y = -x^3$

[fl $(0;0)$; $y=0$]

197) $y = x^4 - x^3$

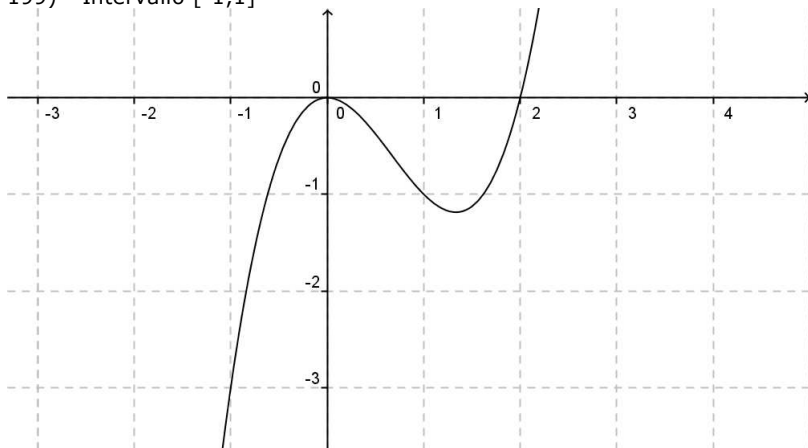
[fl $(0;0)$ $y=0$; fl $(\frac{1}{2}; -\frac{1}{16})$ $y = -\frac{1}{4}x + \frac{1}{16}$]

198) $y = 2x^3 - 3x^2$

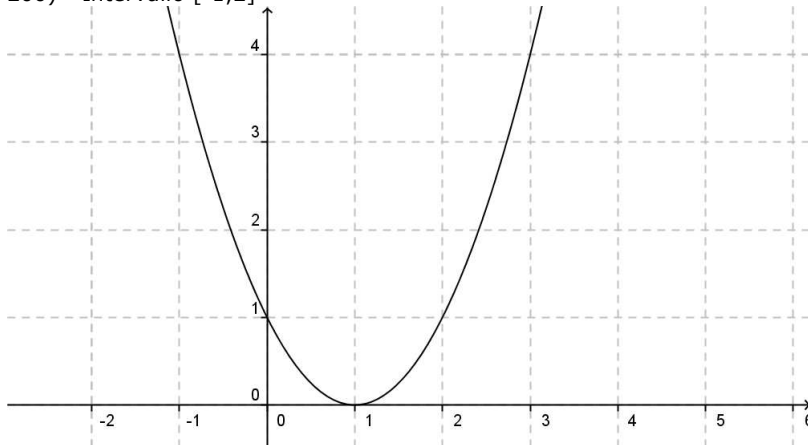
[fl $(\frac{1}{2}; -\frac{1}{2})$; $y = -\frac{3}{2}x + \frac{1}{4}$]

Dire per quali delle seguenti funzioni valgono le ipotesi del teorema di Lagrange, trova il/i punto/i c, disegna la retta passante per A e B e la retta parallela passante per c.

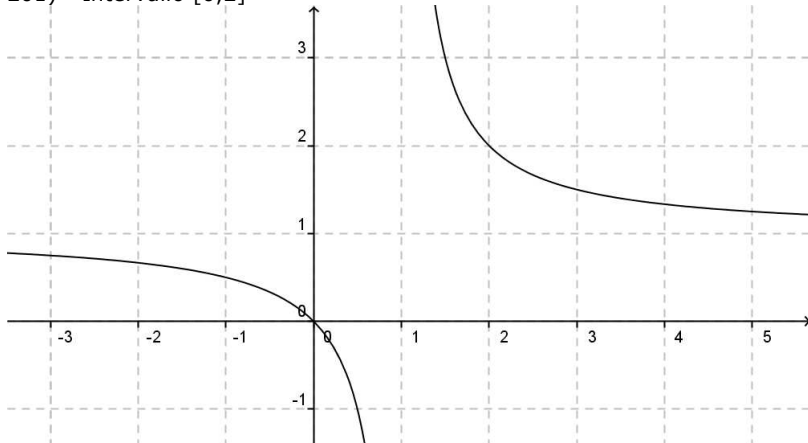
199) Intervallo $[-1,1]$



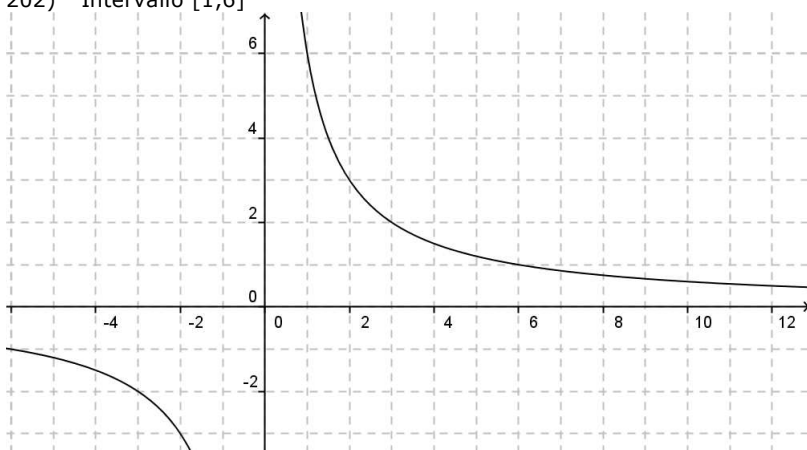
200) Intervallo $[-1,2]$



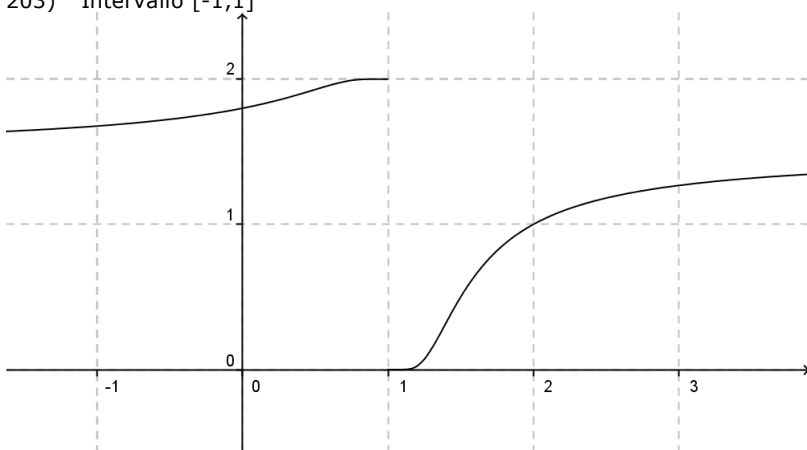
201) Intervallo $[0,2]$



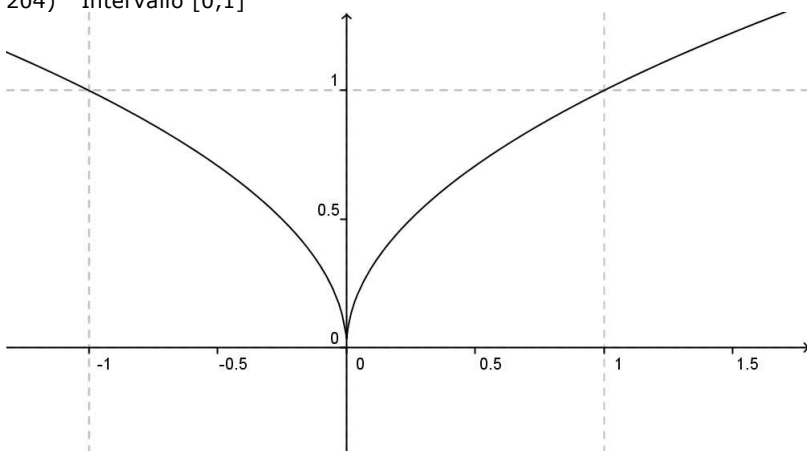
202) Intervallo $[1,6]$



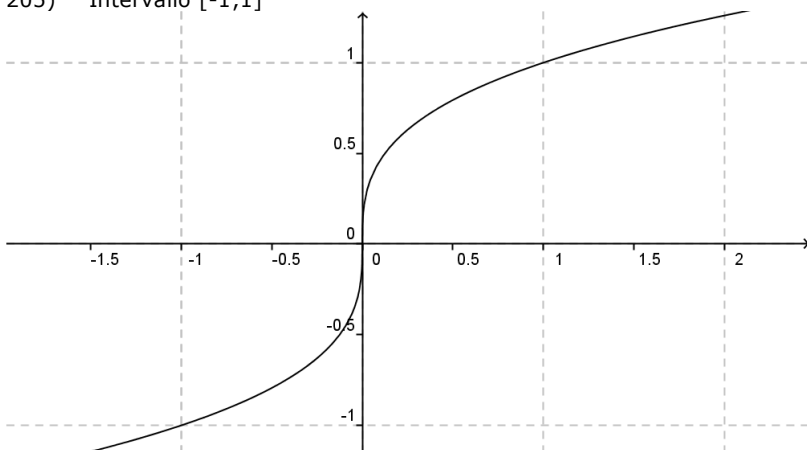
203) Intervallo $[-1,1]$



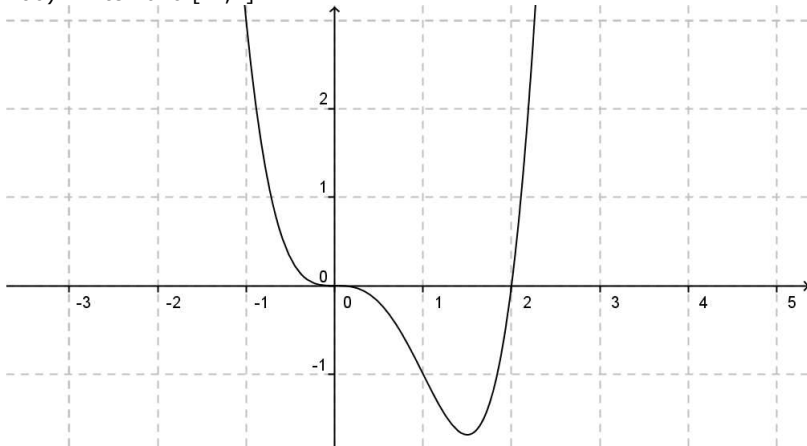
204) Intervallo $[0,1]$



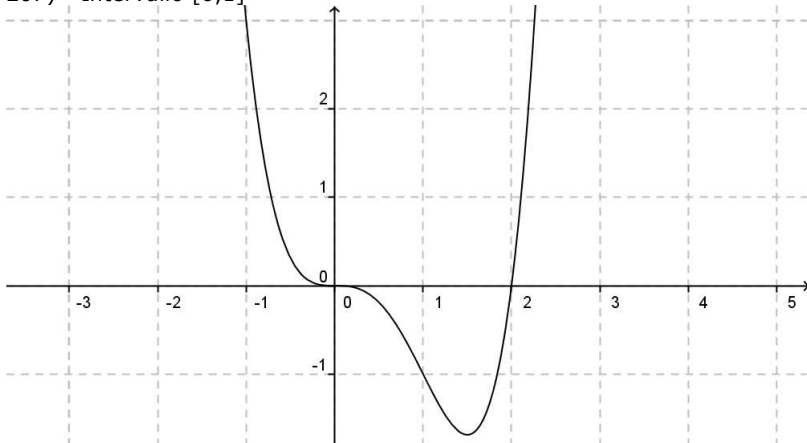
205) Intervallo $[-1,1]$



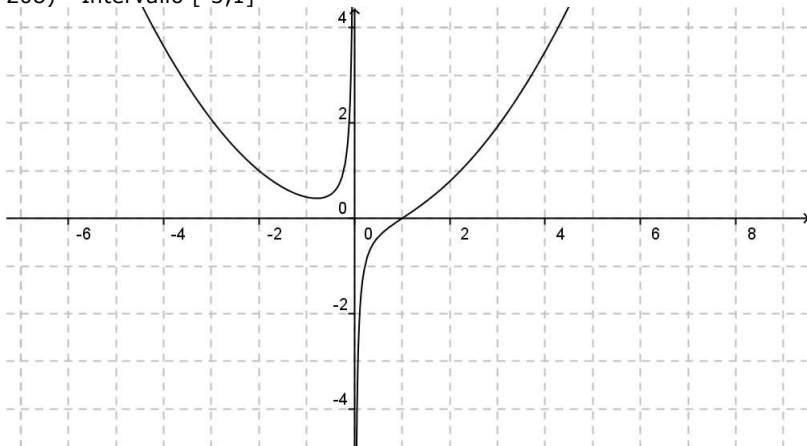
206) Intervallo $[-1,2]$



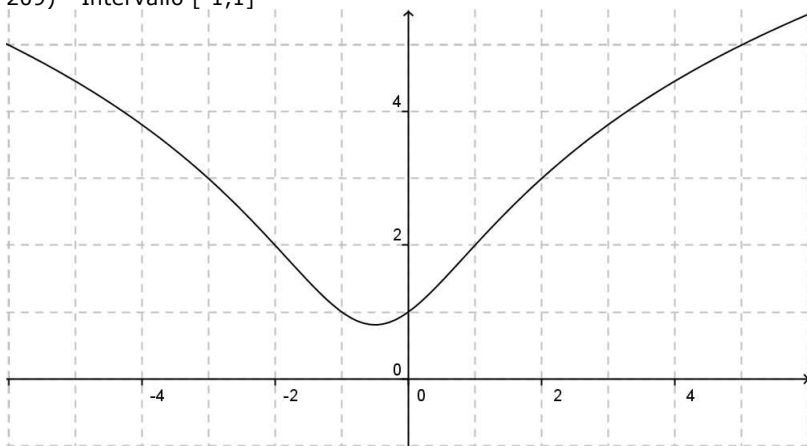
207) Intervallo $[0,1]$



208) Intervallo $[-3,1]$



209) Intervallo $[-1,1]$

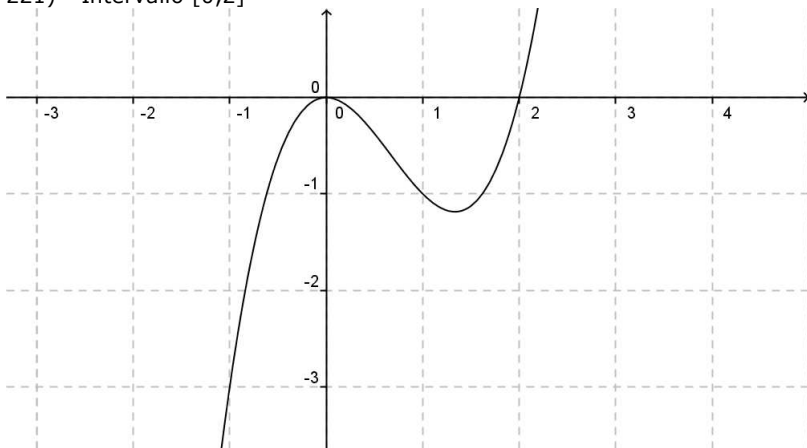


Dire per quali delle seguenti funzioni valgono le ipotesi del teorema di Lagrange e trova il/i punto/i c.

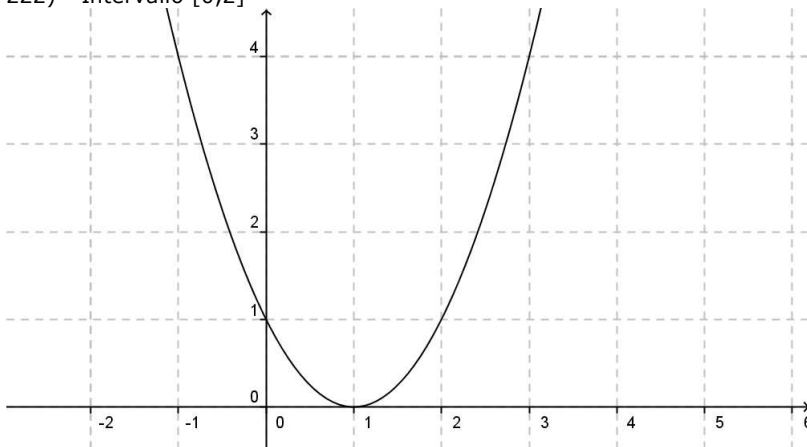
- 210) $y = x^3 - 2x^2$ nell'intervallo $[-1,1]$ $\left[c = \frac{2 - \sqrt{7}}{3} \right]$
- 211) $y = x^2 - 2x + 1$ nell'intervallo $[-1,2]$ $\left[c = \frac{1}{2} \right]$
- 212) $y = \frac{x}{x-1}$ nell'intervallo $[0,2]$ [non vale l'ipotesi di continuità all'interno dell'intervallo]
- 213) $y = \frac{6}{x}$ nell'intervallo $[1,6]$ $\left[c = \frac{5}{2} \right]$
- 214) $y = \frac{6}{3 + 3^{\frac{1}{x-1}}}$ nell'intervallo $[-1,1]$ [non vale l'ip. di continuità agli estremi dell'intervallo]
- 215) $y = \sqrt{|x|}$ nell'intervallo $[0,1]$ $\left[c = \frac{1}{4} \right]$
- 216) $y = \sqrt[3]{x}$ nell'intervallo $[-1,1]$ [non vale l'ipotesi di derivabilità all'interno dell'intervallo ma esistono due c con le caratteristiche richieste, $c_{1,2} = \pm \frac{1}{3}$]
- 217) $y = x^4 - 2x^3$ nell'intervallo $[-1,2]$ [ci sono tre valori di c, è difficile calcolarli algebricamente, approssimativamente valgono 1.36, -0.36, 0.5]
- 218) $y = x^4 - 2x^3$ nell'intervallo $[0,1]$ [c'è un solo valore di c, è difficile calcolarlo algebricamente, approssimativamente vale -0.36]
- 219) $y = \frac{2x^3 - 2}{9x}$ nell'intervallo $[-3,1]$ $\left[c = \sqrt[3]{-\frac{5}{9}} \right]$
- 220) $y = \log_2(x^2 + x + 2)$ nell'intervallo $[-1,1]$ $\left[c = \frac{\ln 2 - 2}{4} \right]$

Dire per quali delle seguenti funzioni valgono le ipotesi del teorema di Rolle, trova il/i punto/i c, disegna la retta tangente alla funzione passante per c.

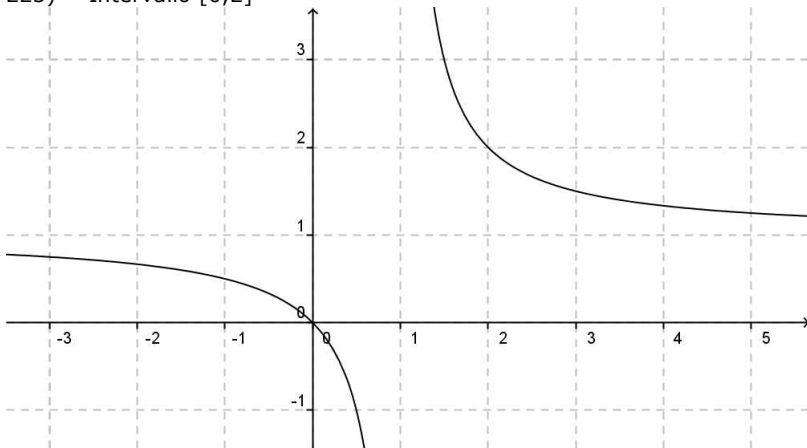
221) Intervallo $[0,2]$



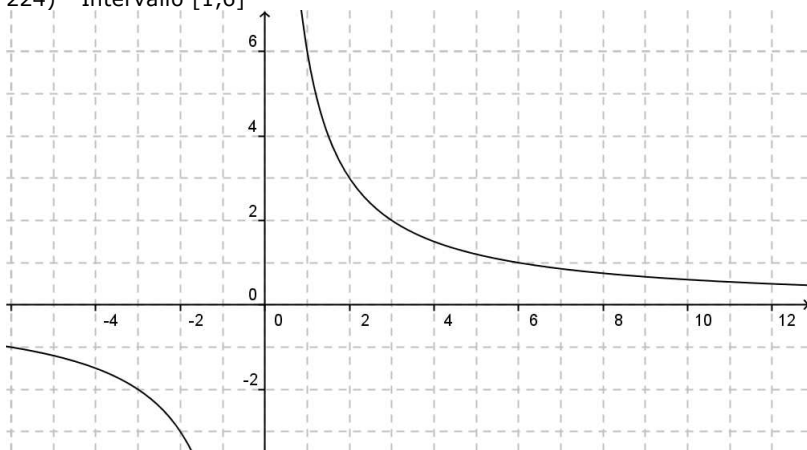
222) Intervallo $[0,2]$



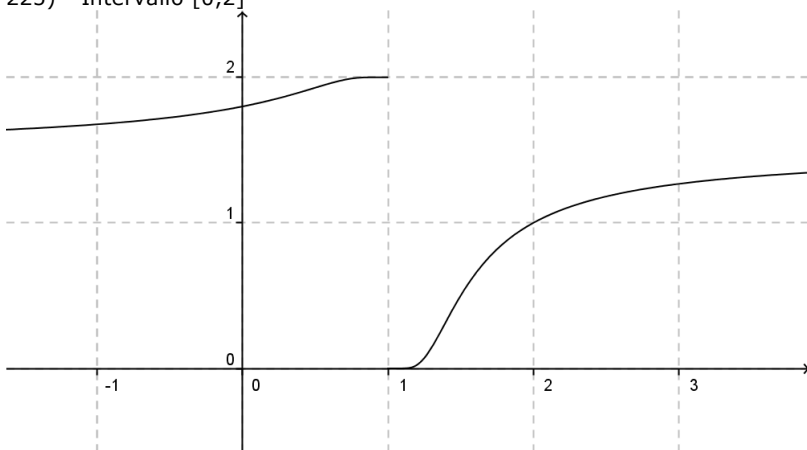
223) Intervallo $[0,2]$



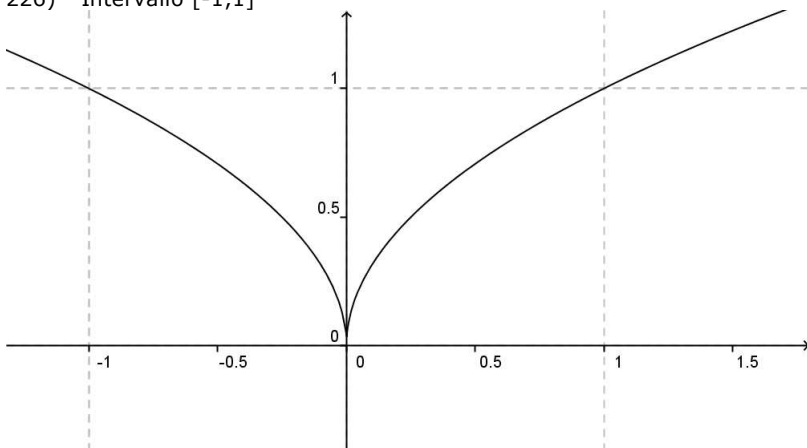
224) Intervallo $[1,6]$



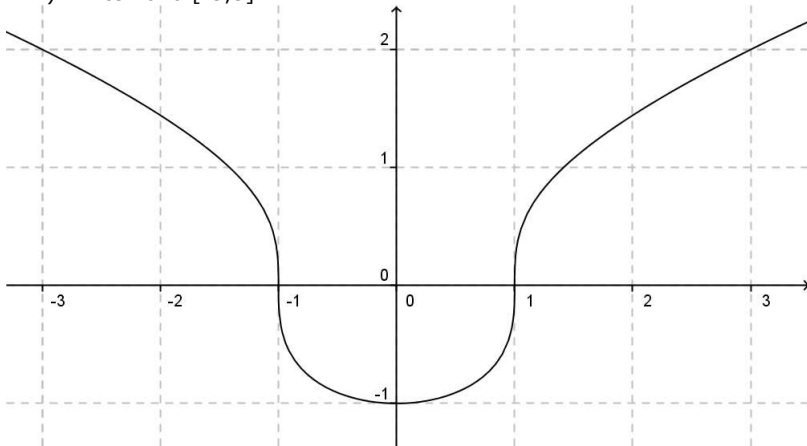
225) Intervallo $[0,2]$



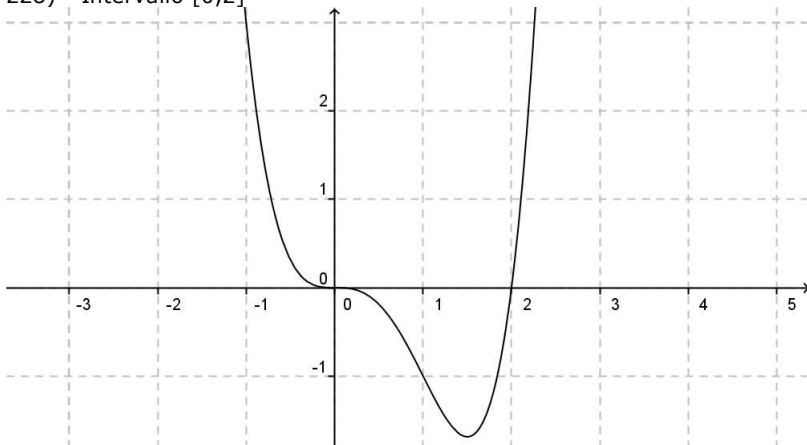
226) Intervallo $[-1,1]$



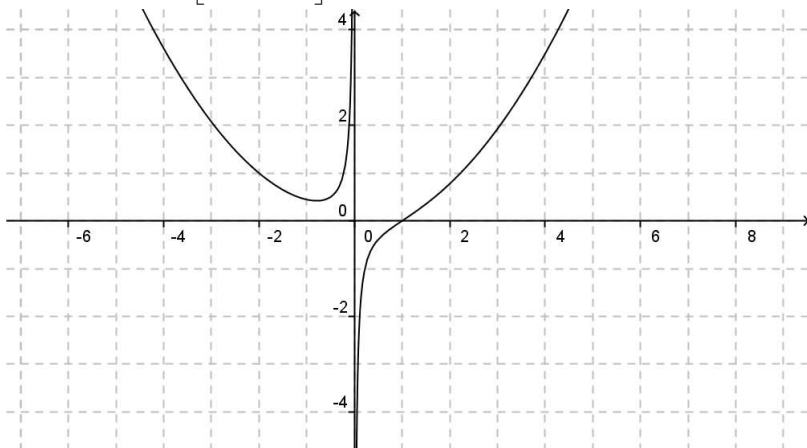
227) Intervallo $[-3,3]$



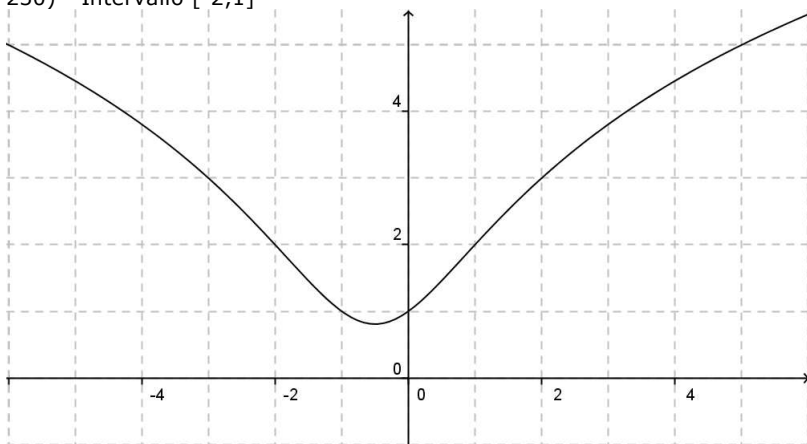
228) Intervallo $[0,2]$



229) Intervallo $\left[-2, \frac{2+\sqrt{6}}{2}\right]$



230) Intervallo $[-2,1]$



Dire per quali delle seguenti funzioni valgono le ipotesi del teorema di Rolle e trova il/i punto/i c.

- 231) $y = x^3 - 2x^2$ nell'intervallo $[0,2]$ $\left[c = \frac{4}{3} \right]$
- 232) $y = x^2 - 2x + 1$ nell'intervallo $[0,2]$ $[c = 1]$
- 233) $y = \frac{x}{x-1}$ nell'intervallo $[0,2]$ [non vale l'ipotesi di continuità all'interno dell'intervallo]
- 234) $y = \frac{6}{x}$ nell'intervallo $[1,6]$ [non vale l'ipotesi $f(a)=f(b)$]
- 235) $y = \frac{6}{3 + 3^{\frac{1}{x-1}}}$ nell'intervallo $[0,2]$ [non vale l'ipotesi di continuità all'interno dell'intervallo]
- 236) $y = \sqrt{|x|}$ nell'intervallo $[-1,1]$ [non vale l'ip. di derivabilità all'interno dell'intervallo]
- 237) $y = \sqrt[3]{x^2 - 1}$ nell'intervallo $[-3,3]$ [non vale l'ip. di derivabilità all'interno dell'intervallo, ciò nonostante esiste $c=0$ con le caratteristiche richieste]
- 238) $y = x^4 - 2x^3$ nell'intervallo $[0,2]$ $\left[c = \frac{3}{2} \right]$
- 239) $y = \frac{2x^3 - 2}{9x}$ nell'intervallo $\left[-2, \frac{2 + \sqrt{6}}{2} \right]$ [non vale l'ip. di continuità all'interno dell'intervallo, ciò nonostante esiste $c=0$ con le caratteristiche richieste $c = \sqrt[3]{-\frac{1}{2}}$]
- 240) $y = \log_2(x^2 + x + 2)$ nell'intervallo $[-2,1]$ $\left[c = -\frac{1}{2} \right]$

241) Data $y=f(x)$ continua in $[a,b]$ e derivabile in $]a,b[$, non è detto che esista un punto $c \in]a,b[$ tale che $f'(c)=0$.
Si mostri il grafico di una funzione continua in $[a,b]$ e derivabile in $]a,b[$ per cui non esista un punto c tale che $f'(c)=0$, e il grafico di un'altra funzione continua in $[a,b]$ e derivabile in $]a,b[$ per cui esista un punto c tale che $f'(c)=0$.

242) Data $y=f(x)$ continua in $]a,b[$, derivabile in $]a,b[$ con $f(a)=f(b)$, non è detto che esista un punto $c \in]a,b[$ tale che $f'(c)=0$.
Si mostri il grafico di una funzione continua in $]a,b[$ e derivabile in $]a,b[$ con $f(a)=f(b)$, per cui non esista un punto c tale che $f'(c)=0$, e il grafico di un'altra funzione continua in $]a,b[$ e derivabile in $]a,b[$ con $f(a)=f(b)$, per cui esista un punto c tale che $f'(c)=0$.

243) Data $y=f(x)$ continua in $[a,b]$ a parte $x_0 \in]a,b[$ punto di discontinuità, derivabile in $]a,b[\setminus\{x_0\}$, con $f(a)=f(b)$, non è detto che esista un punto $c \in]a,b[$ tale che $f'(c)=0$.
Si mostri il grafico di una funzione continua in $[a,b]$ a parte $x_0 \in]a,b[$ punto di discontinuità e derivabile in $]a,b[\setminus\{x_0\}$, con $f(a)=f(b)$, per cui non esista un punto c tale che $f'(c)=0$, e il grafico di un'altra funzione continua in $[a,b]$ a parte $x_0 \in]a,b[$ punto di discontinuità e derivabile in $]a,b[\setminus\{x_0\}$, con $f(a)=f(b)$, per cui esista un punto c tale che $f'(c)=0$.

244) Data $y=f(x)$ continua in $]a,b[$, derivabile in $]a,b[\setminus\{x_0\}$ con $f(a)=f(b)$ e x_0 punto di non derivabilità, non è detto che esista un punto $c \in]a,b[$ tale che $f'(c)=0$.
Si mostri il grafico di una funzione continua in $]a,b[$, derivabile in $]a,b[\setminus\{x_0\}$ con $f(a)=f(b)$ e x_0 punto di non derivabilità, per cui non esista un punto c tale che $f'(c)=0$, e il grafico di un'altra funzione continua in $]a,b[$, derivabile in $]a,b[\setminus\{x_0\}$ con $f(a)=f(b)$ e x_0 punto di non derivabilità, per cui esista un punto c tale che $f'(c)=0$.